CH302 Spring 2009 Worksheet 1 Answer Key: A Little Thermo Review

- 1. What two processes (a.k.a. path functions) can transfer internal energy between a system and its surroundings? What symbols are used for these variables? Heat and work. q for heat and w for work.
- 2. Write a good definition for a state function.

A state function is a property of a system which is dependent exclusively on the state of the system and not the processes leading to that state.

3. Name some state functions.

Temperature, Volume, Pressure, Number of Moles, Gibb's Free Energy, Entropy, Enthalpy, Internal Energy, etc.

4. The first law states that the value of which state function is conserved in an isolated system? What **two** symbols are used for this state function?

Internal energy (E or U).

5. What is an isolated system? Name the most obvious example of an isolated system (hint: big).

A closed system is one that exchanges neither matter nor energy with its surroundings. The universe is the most obvious example because it has no surroundings.

6. What **inequality** is often associated with the second law of thermodynamics? What does it mean in plain English?

 $\Delta G_{univ} > 0$. This means that the entropy of the universe is always increasing.

7. What **equality** is often associated with the second law of thermodynamics? What does it mean in plain English?

 $\Delta G_{univ} = \Delta G_{system} + \Delta G_{surroundings}$. This means that the universe's change in entropy is the sum of the system's and surrounding's change in entropy

8. What does the third law of thermodynamics state?

It states that the entropy of a perfect crystal will approach zero as its temperature approaches zero.

- 9. How many translational, rotational and vibrational modes, respectively, does C₂H₄ have? It has 3 translational, 2 rotational, and 13 vibrational modes.
- 10. What would be the total internal energy associated with the vibrational motion of 1 molecule of C_2H_4 ? What about 1 mole of C_2H_4 ?

since E = 0.5kT for each mode, one molecule would have 6.5kT and one mole 6.5RT.

11. In the list of elements below, mark (circle, underline, etc.) all of the elements that are not shown in their standard state.

12. Write the standard formation reactions for the following chemical species NH₃(q)

$$1/2N_2(g) + 3/2H_2(g) \rightarrow NH_3(g)$$

 $Fe_2O_3(s)$
 $2Fe(s) + 3/2O_2(g) \rightarrow Fe_2O_3(s)$
 $O_2(I)$

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O_2(g) \rightarrow O_2(I)

O_3(g)

3/2O_2(g) \rightarrow O_3(g)

NH_2OH(s)

1/2N_2 + 3/2H_2 + 1/2O_2 \rightarrow NH_2OH(s)
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13. Assume we want to use a bomb calorimeter to determine the specific heat capacity of an unknown liquid. We use 3 L of the unkown liquid and perform a known reaction that releases 400 kJ of heat. We measure an initial and final temperature of 25 °C and 28.7 °C, respectively. If the heat capacity of the calorimeter is 85 J·K⁻¹, and the density of the liquid is 2.34 g·mL⁻¹, what is the specific heat capacity of the unknown liquid?

$$\begin{split} \Delta H &= 400 \text{ kJ} \\ m &= 3 \text{ L} * 1000 \text{ mL} \cdot \text{L}^{-1} * 2.34 \text{ g} \cdot \text{mL}^{-1} = 7020 \text{ g} \\ \Delta T &= T_f \cdot T_i = 28.7 \text{ °C} \cdot 25 \text{ °C} = 3.7 \text{ °C} = 3.7 \text{ K} \\ c_{cal} &= 85 \text{ J} \cdot \text{K}^{-1} * .001 \text{ kJ} \cdot \text{J}^{-1} = 0.085 \text{ kJ} \cdot \text{K}^{-1} \\ \Delta H &= m \cdot c \cdot \Delta T + c_{cal} \cdot \Delta T \\ c &= (\Delta H \cdot c_{cal} \cdot \Delta T) / (m \cdot \Delta T) \\ &= (400 \text{ kJ} \cdot 0.085 \text{ kJ} \cdot \text{K}^{-1} * 3.7 \text{ K}) / (7020 \text{ g} * 3.7 \text{ K}) \\ &= 0.01539 \text{ kJ} \cdot \text{g}^{-1} \cdot \text{K}^{-1} = 15.39 \text{ J} \cdot \text{g}^{-1} \cdot \text{K}^{-1} \end{split}$$

14. Given the following data:

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H_2SO_4(I) \leftrightarrow H_2S(g) + 2O_2(g) \Delta H = 793 \text{ kJ·mol}^{-1}

H_2O(g) + SO_3(g) \leftrightarrow H_2SO_4(I) \Delta H = -176 \text{ kJ·mol}^{-1}

H_2O(I) + SO_3(g) \leftrightarrow H_2S(g) + 2O_2(g) \Delta H = 661 \text{ kJ·mol}^{-1}

calculate \Delta H for the process: H_2O(I) \rightarrow H_2O(g)

\Delta H = (-1*793 \text{ kJ·mol}^{-1}) + (---**-173 \text{ kJ·mol}^{-1}) + (1*661 \text{ kJ·mol}^{-1})

= 41 \text{ kJ·mol}^{-1}
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15. Consider the reaction below and approximate the value of the work function at room temperature. (Note: this doesn't require a calculator.)

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C_2H_4(g) + 3O_2(g) \rightarrow 2CO_2(g) + 2H_2O(l)
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At room temperature (\sim 300K), the product of the RT term in w = $-\Delta n_{gas}$ RT is approximately 2.5 kJ. Since Δn_{gas} is -2 for this reaction, the work function is approximately 5 kJ.

- 16. If a system at -272 °C absorbs 545 J of heat, what is its change in entropy? 545 J·K⁻¹
- 17. Ammonia (the common name for NH₃, the odor of windex and cat urine), has a $\Delta H^{o}_{vap} = 23.35 \text{ kJ} \cdot \text{mol}^{-1}$ and a $\Delta S^{o}_{vap} = 97.43 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$. What is the normal boiling point of ammonia expressed in centigrade?

Because boiling is an equilibrium process, $\Delta G^{\circ}_{vap} = 0 = \Delta H^{\circ}_{vap} - T\Delta S^{\circ}_{vap}$. And so $T\Delta S^{\circ}_{vap} = \Delta H^{\circ}_{vap}$ and $T = \Delta H^{\circ}_{vap}/\Delta S^{\circ}_{vap} = 23,350 \text{ J} \cdot \text{mol}^{-1}/97.43 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1} = 238.7 \text{ K} = -33.3 \text{ °C}$.

18. Consider the reaction below:

$$HNO_3(I) + H_2(g) \leftrightarrow H_2O(I) + NO_2(g)$$

Using the provided table values, calculate ΔG^{o}_{rxn} if it is performed under standard conditions.

$$\Delta H^{\circ}_{f}$$
 ΔS°_{m} $(kJ \cdot mol^{-1})$ $(J \cdot mol^{-1} \cdot K^{-1})$

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H<sub>2</sub>(g) not provided 131

H<sub>2</sub>O(l) -285.8 70

NO<sub>2</sub>(g) 33.2 240

ΔH<sub>rxn</sub> = ΣH<sub>f</sub>,products - ΣH<sub>f</sub>,reactants

= (-285.8 kJ·mol<sup>-1</sup> + 33.2 kJ·mol<sup>-1</sup>) - (-174.10 kJ·mol<sup>-1</sup>)

= -78.5 kJ·mol<sup>-1</sup>

ΔS<sub>rxn</sub> = ΣS<sub>m</sub>,products - ΣS<sub>m</sub>,reactants

= (70 J·mol<sup>-1</sup>·K<sup>-1</sup> + 240 J·mol<sup>-1</sup>·K<sup>-1</sup>) - (156 J·mol<sup>-1</sup>·K<sup>-1</sup> + 131 J·mol<sup>-1</sup>·K<sup>-1</sup>)

= 23 J·mol<sup>-1</sup>·K<sup>-1</sup> = 0.023 kJ·mol<sup>-1</sup>·K<sup>-1</sup>

ΔG°<sub>rxn</sub> = ΔH°<sub>rxn</sub> - TΔS°<sub>rxn</sub>

= -78.5 kJ·mol<sup>-1</sup> - 273 K*0.023 J·mol<sup>-1</sup>·K<sup>-1</sup>

= -85 kJ·mol<sup>-1</sup>
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20. Assuming you have one mole of each of the following, rank them in terms of decreasing value of the term W in the Boltzmann equation: HF, NaF, CIF, F₂.

 $CIF > HF > NaF > F_2$

 $CO_2(g) > CO_2(I) > CO(I) > CO(s)$

 $CO_2(g)$, $CO_2(I)$, CO(I).

HNO₃(I)

-174.1

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